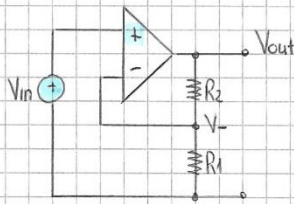


# FORMULARIO

(1)

## Amplificatore ideale

### CONFIGURAZIONE NON INVERTENTE

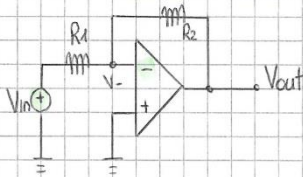


$$V_{in} = V_+ = V_- = V_{out} \frac{R_1}{R_1 + R_2} = \beta V_{out}$$

$$\frac{V_{out}}{V_{in}} = \frac{1}{\beta}$$

$$\beta = \frac{R_1}{R_1 + R_2}$$

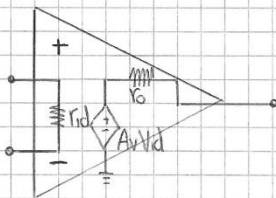
### CONFIGURAZIONE INVERTENTE



$$\frac{V_{in} - V_-}{R_1} = \frac{V_- - V_{out}}{R_2} \quad \text{e} \quad V_- = V_+ = 0$$

$$\frac{V_{out}}{V_{in}} = -\frac{R_2}{R_1}$$

## Amplificatore reale



$$\text{con } V_{id} = V_+ - V_-$$

$R_{if}$  : resistenza d'ingresso

$R_{of}$  : resistenza d'uscita

con l'incremento di:

$$\Delta V_x \quad R = \frac{V_x}{I_x}$$

NON INVERTENTE  $R_{if} = R_{id}(1 + A_0\beta)$   
 $R_{of} = \frac{R_o}{(1 + A_0\beta)} \parallel (R_1 + R_2)$

INVERTENTE  $R_{if} = R_1 + \frac{R_2 + R_o}{1 + A_0} \parallel R_{id}$

Il guadagno è dipendente dalla frequenza  $A = A(\omega)$

(da il problema)  
 $A_0$ : guadagno in continua

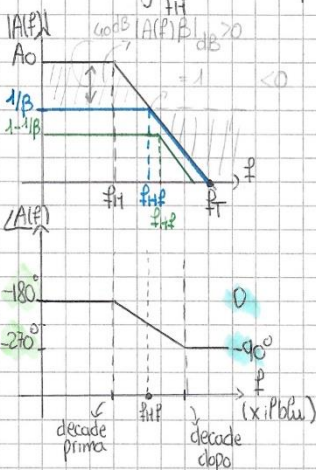
$f_H$ : frequenza di taglio a 3dB

$$A_0 = \frac{1}{\beta} \frac{\beta A_0}{1 + \beta A_0} \sim \frac{1}{\beta}$$

$$A_0 = \left( \frac{1}{\beta} + 1 \right) \frac{\beta A_0}{1 + \beta A_0} \sim 1 - \frac{1}{\beta}$$

$$dB = 20 \log(x)$$

$$x = 10^{\frac{dB}{20}}$$



$$f_T: \text{freq di taglio } |A(f)| = 1 \sim \frac{A_0 f_H}{f_T} = 1$$

$|A|$  guadagno ad anello

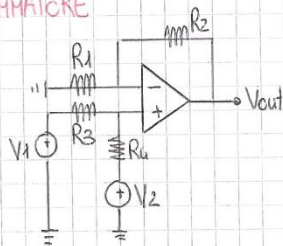
polo -20dB  
 zero +20dB

$$\frac{V_{out}}{V_{in}} = A(f) = A_0 \frac{1}{1 + j \frac{f}{f_H(1 + \beta A_0)}}$$

(Vica Vo io)

Ao con retroazione negativa

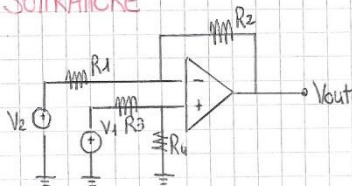
SOMMATTORE



$$V_{out}(t) = d_1 V_1(t) + d_2 V_2(t)$$

$$\text{con } d_1 = \left(1 + \frac{R_2}{R_1}\right) \frac{R_4}{R_3 + R_4} \quad \text{e } d_2 = \left(1 + \frac{R_2}{R_1}\right) \frac{R_3}{R_3 + R_4}$$

SOTTRATTORE

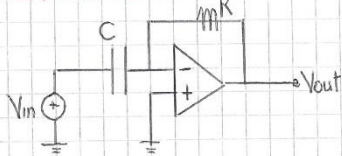


$$V_{out}(t) = d_1 V_1(t) - d_2 V_2(t)$$

$$A_o = 1/\beta$$

$$\text{con } d_1 = \frac{R_4}{R_3 + R_4} \frac{R_1 + R_2}{R_1} \quad d_2 = \frac{R_2}{R_1}$$

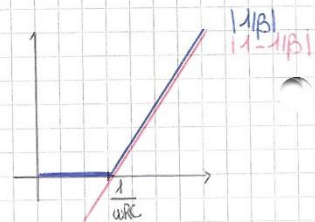
DERIVATORE



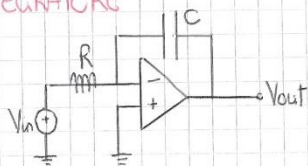
$$V_{out}(t) = -CR \frac{dV_{in}(t)}{dt}$$

$$\beta = \frac{1/j\omega C}{R + 1/j\omega C}$$

$$\frac{V_{out}}{V_{in}} = 1 - \frac{1}{\beta}$$



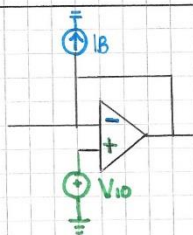
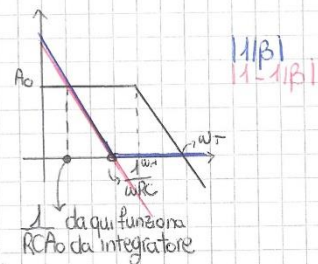
INTEGRATORE



$$V_{out}(t + t_0) = -\frac{1}{RC} \int_{t_0}^{t+t_0} V_{in}(\tau) d\tau + V_{out}(t_0)$$

$$\beta = \frac{R}{R + 1/j\omega C}$$

$$\frac{V_{out}}{V_{in}} = 1 - \frac{1}{\beta}$$



CORRENTE DI POLARIZZAZIONE ⊖

TENSIONE DI OFFSET ⊕

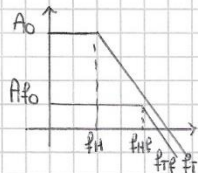
$$I_C = C \frac{dV_C(t)}{dt}$$

$$V_C(t) = \int_0^t \frac{I_C}{C} dt$$

• Trova la funzione di trasferimento  $V_{out}/V_{in}$

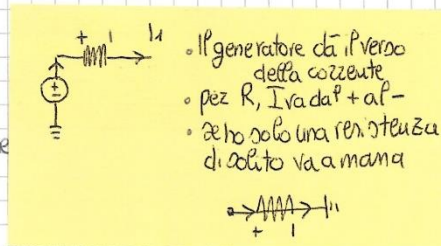
• tracciano i diagrammi di Bode di modulo e fase avendo  $A(f) = \frac{A_0}{1+j\frac{f}{f_H}}$

=> devo trovare  $A_0 \Rightarrow \frac{1}{\beta} \frac{\beta A_0}{1+\beta A_0}$  guadagno



$$f_{HF} = f_H(1+\beta A_0) \quad f. \text{ di taglio}$$

$$f_T: \frac{A_0 \cdot f_H}{f_T} = 1 \quad f. \text{ di trasmissione (GBW)}$$

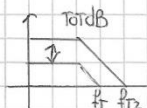


• Progettare... scegli il valore delle resistenze => sistema di equazioni.

+ banda passante: si calcola  $\beta$

+ SLEW RATE:  $SR \gg \left| \frac{dV_{out}(t)}{dt} \right|_{MAX}$  (di solito  $V_{out}(t) = V_0 \sin(2\pi f_0 t)$ )

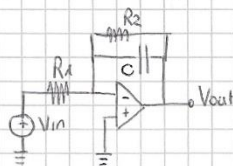
+ guadagno di anello



$$f_{T2} = f_T \cdot T_0 \text{ assoluto}$$

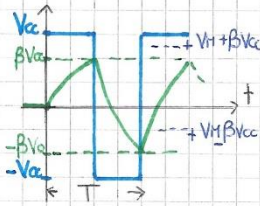
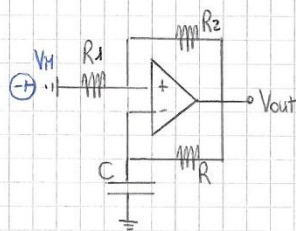
+ se chiedevi valutare un amplificatore, devo guardare  $f_T$

+ quando non mi viene dato il circuito



## Ao con retroazione positiva

### Multivibratore astabile

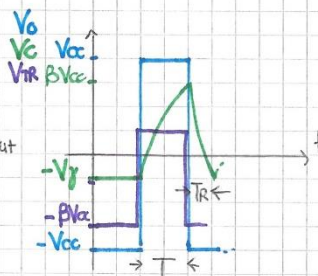
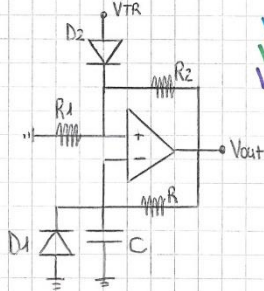


$V_{out}$   
 $V_c$

$$T = 2RC \ln \left( \frac{1+\beta}{1-\beta} \right)$$

$$* T_1 = RC \ln \left( \frac{1+\beta - V_H/V_{cc}}{1-\beta - V_H/V_{cc}} \right) \neq T_2 \frac{1+\beta}{1-\beta}$$

### Multivibratore monostabile



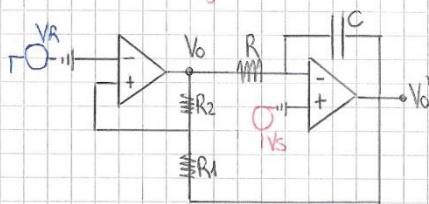
$$T = RC \ln \left( \frac{1 + V_H/V_{cc}}{1 - \beta} \right)$$

$$T_R = RC \ln \left( \frac{1+\beta}{1 - V_H/V_{cc}} \right)$$

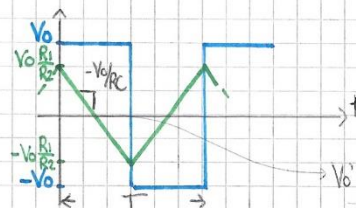
\* per impulsi  
negativi



### Generatore di onda triangolare



$V_+ = 0$  commuta



$V_0$   $V_0'$

$$T = 4RC \frac{R_1}{R_2}$$

$$V_0'(T/2) = V_0'(0) - \frac{V_0}{RC} \frac{T}{2}$$

\* cambia  
l'ampiezza

$$V_R + V_0 \frac{R_1}{R_2}$$

$$V_R - V_0 \frac{R_1}{R_2}$$

\* cambiano i periodi

$$T_1 = \frac{2V_0}{V_0 - V_S} \frac{R_1 RC}{R_2}$$

$$T_2 = \frac{2V_0}{V_0 + V_S} \frac{R_1 RC}{R_2}$$

## Convertitori A/D e D/A

(6)

### Generale

- massima frequenza del segnale in ingresso per rispettare il teorema del campionamento

$$f_c = \frac{1}{T_c} \quad T_c = T_{\text{campionamento}} = T_{\text{acquisizione}} + T_{\text{conversione}} \Rightarrow \text{Trovo } B$$

- massimo errore di quantizzazione

$$V_{\text{LSB}} = \frac{V_{\text{FS}}}{2^n}$$

$n$ : bit

$V_{\text{FS}}$ : fondo scala

• ARROTONDAMENTO

$$\left\lfloor \frac{V_{\text{LSB}}}{2} \right\rfloor$$

• TRONCAMENTO

- massimo rapporto segnale-rumore

$$\text{SNR}_{\text{dB}} = n \cdot 6,02 + 1,76 \text{ (ARR)}$$

• half flash

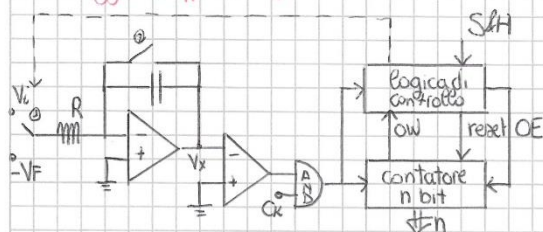
•

- 4,25 (TRONC)

• a conteggio (doppia rampa)  
• SAR

### A/D

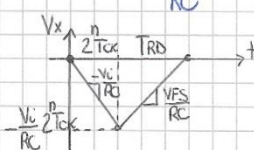
#### a. conteggio (doppia rampa)



$n$  bit,  $V_i \in [0; V_{\text{FS}}]$

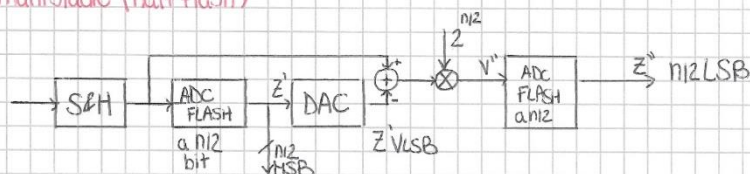
- $2^n T_{\text{CK}} = n T_{\text{noise}}$
- $V_{\text{out}} = -\frac{V_i}{RC} + n_{\text{noise}}$

- $T_{\text{conversione}} = 2 \cdot 2^n T_{\text{CK}}$
- $RC$ : costante di tempo dell'integratore

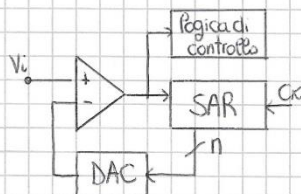


$$T_c = T_{\text{setting}} + T_{\text{acquisizione}} + 2^n T_{\text{CK}} + n T_{\text{noise}} \quad \text{non sono di cui}$$

#### multistadio (half flash)



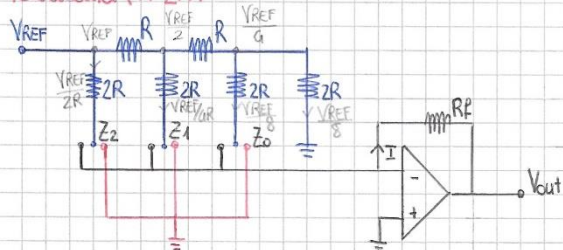
#### approssimazioni successive (SAR)



$$T_{\text{conversione}} = n T_{\text{CK}}$$

D/A

retroscala (R-2R)

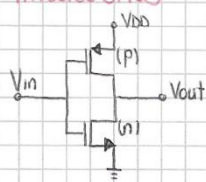


$$V_{out} = -I R_f \quad I = \frac{V_{REF}}{2} \left[ Z_2 + \frac{Z_1}{2} + \frac{Z_0}{4} \right]$$

$$\Rightarrow V_{out} = -\frac{V_{REF}}{8} \frac{R_f}{R} [4Z_2 + 2Z_1 + Z_0]$$

## Inverter CMOS

(5)



$$K_n = \frac{1}{2} \mu_n C_{ox} \frac{W_n}{L_n} [A/V^2] \quad \text{con } C_{ox} = \frac{\epsilon_{ox}}{t_{ox}}$$

• tensione di soglia logica

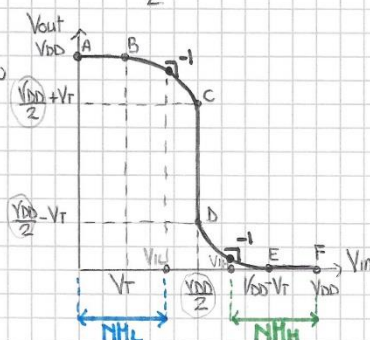
$$K_n (V_i - V_{TH})^2 = K_p (V_{DD} - V_i - V_{TH})^2 \Rightarrow \text{Trova } V_i (V_{SL})$$

• tempo di propagazione

$$t_{p_{LH}} = \frac{\frac{V_{DD}}{2} \cdot C_L}{K_p (V_{DD} - V_{TH})^2} \left( n_{in \text{ a c.c.}} \right) \quad t_{p_{HL}} = \frac{\frac{V_{DD}}{2} \cdot C_L}{K_n (V_{DD} - V_{TH})^2} \left( n_{in \text{ a c.c.}} \right)$$

$$t_p = \frac{t_{p_{LH}} + t_{p_{HL}}}{2}$$

• Caratteristica di trasferimento



•  $V_{SL}$

• Margini di rumore

$$NMH = V_{DD} - V_{THmin} = NHL$$

• Potenza dissipata dinamica

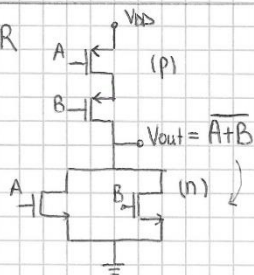
$$P_D = N C_L V_{DD}^2 f$$

• Corrente di picco ( $V_i = V_{DD}/2$ )

$$I_p = K_n (V_i - V_{TH})^2$$

statica  $P_D = \frac{1}{2} V_{DD} I_D$  (equiprobabile)

NOR

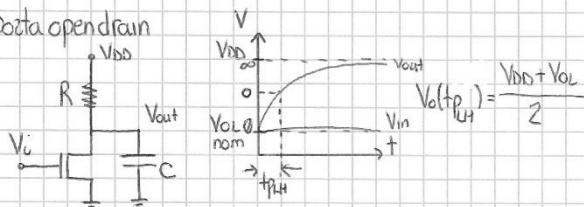


• p e n sono "simmetrici", prima a fa n, e poi p

+ : in parallelo

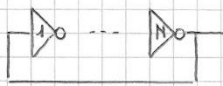
• : in serie

porta open drain



$$V_o(t) = [V_o(\infty) - V_o(0)](1 - e^{-t/RC}) + V_o(0)$$

oscillatore ad anello



$$T = (t_{PLH} + t_{PHL}) \cdot N$$

Memoria

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